The stomatal response to rising CO₂ concentration and drought is predicted by a hydraulic trait-based optimization model

Yujie Wang¹*, John S. Sperry¹, Martin D. Venturas¹, Anna T. Trugman¹, David M. Love¹,², and William R. L. Anderegg¹

¹ School of Biological Sciences, University of Utah, Salt Lake City, 257S 1400E, Utah 84112, USA
² Warnell School of Forestry and Natural Resources, University of Georgia, 180 E Green Street, Athens, GA 30602-2152, USA

* Author for correspondence: yujie.wang@utah.edu

The present study is a revision for TP-2018-481.

Short summary: This study tested a trait-based model that optimizes photosynthesis gain and hydraulic risk. The gain-risk model predicted the stomatal response to environmental cues such as CO₂ concentration, atmospheric humidity, and soil drought. A comparison indicated that the gain-risk model outperformed a widely used empirical approach fitted to the same dataset.

Keywords: CO₂ concentration, drought, gain-risk optimization model, gas exchange, hydraulic risk, stomatal control

Running Title: Trait-based model predicts stomatal behavior
Abstract

Modeling stomatal control is critical for predicting forest responses to the changing environment and hence the global water and carbon cycles. A trait-based stomatal control model that optimizes carbon gain while avoiding hydraulic risk has been shown to perform well in response to drought. However, the model’s performance against changes in atmospheric CO₂, which is rising rapidly due to human emissions, has yet to be evaluated. The present study tested the gain-risk model’s ability to predict the stomatal response to CO₂ concentration with potted water birch (Betula occidentalis Hook.) saplings in a growth chamber. The model’s performance in predicting stomatal response to changes in atmospheric relative humidity and soil moisture was also assessed. The gain-risk model predicted the photosynthetic assimilation, transpiration rate, and leaf xylem pressure under different CO₂ concentrations, having a mean absolute percentage error (MAPE) of 25%. The model also predicted the responses to relative humidity and soil drought with the MAPE of 21.9% and 41.9%, respectively. Overall, the gain-risk model had a MAPE of 26.8% compared to the 37.5% MAPE obtained by a standard empirical model of stomatal conductance. Importantly, unlike empirical models, the optimization model relies on measurable physiological traits as inputs and performs well in predicting responses to novel environmental conditions without empirical corrections.

Incorporating the optimization model in larger scale models has the potential for improving the simulation of water and carbon cycles.

Keywords: CO₂ concentration, drought, gain-risk optimization model, gas exchange, hydraulic risk, stomatal control
Introduction

During the past 60 years, atmospheric CO2 concentration has increased from 314 to 410 ppm. This accumulation of greenhouse gas has led to 0.85 °C increase in the global mean annual temperature (IPCC 2014). The rapid temperature increase has likely exacerbated drought stress on forests in many regions, leading to episodes of drought-induced tree mortality across the globe (Adams et al. 2009, Allen et al. 2010). However, concurrent atmospheric CO2 fertilization may mitigate the negative temperature effects on drought (Zinta et al. 2014, AbdElgawad et al. 2015, Gonzalez-Benecke et al. 2017). Fully understanding and predicting the outcomes of climate change and CO2 fertilization on terrestrial ecosystems is contingent on models that can be used to predict responses to novel future environments (Katul et al. 2009, 2010, Medlyn et al. 2011, Chen et al. 2012, Mcdowell et al. 2013, Mackay et al. 2015, Anderegg et al. 2017, Tai et al. 2017).

A critical modeling challenge is how to represent the complexity of stomatal behavior which influences plant water loss and CO2 uptake. To date, most land surface models rely on empirical representations of stomatal responses to environmental cues based on curve fitting to existing data sets (Ball et al. 1987, Leuning 1995, Tuzet et al. 2003, De Kauwe et al. 2013, Walker et al. 2014, Drake et al. 2017). The empirical models are computationally efficient and do not require an understanding of the complex mechanisms underlying stomatal regulation (Chen et al. 2012, Hills et al. 2012). However, the fitted parameters of these models lack physiological or physical identities, and cannot be derived explicitly from measurable plant traits (Anderegg et al. 2016, Sperry et al. 2017). Consequently, the empirical approach has a strong risk of being inadequate for accurately predicting plant responses to novel conditions (Powell et al. 2013, Anderegg et
These models also do not directly predict the impact of drought stress on the plant’s vascular transport system, the damage of which is strongly linked to the plants’ drought responses and mortality risk (Sperry and Love 2015, Sperry et al. 2016, Adams et al. 2017, Trugman et al. 2018a). As an alternative to the strictly empirical approach, a goal-oriented solution for stomatal behavior is potentially powerful, i.e. assuming that plants optimize water use relative to photosynthetic gain. A commonly used approach is the Water Use Efficiency Hypothesis (WUEH), which maximizes the photosynthetic gain for a given amount of water during a given time period (Cowan and Farquhar 1977). This WUEH model is a “constrained-optimization” problem without an exact solution (Katul et al. 2009, 2010, Wolf et al. 2016, Buckley et al. 2017) and often struggles to predict accurate response to \([\text{CO}_2]\) and soil moisture (Buckley and Schymanski 2014, Buckley 2017). The WUEH holds that stomata regulate to maintain a constant marginal water use efficiency, \(\lambda\). Katul et al. (2009, 2010) solved the optimal stomatal conductance as a function of atmospheric humidity, atmospheric \([\text{CO}_2]\), and \(\lambda\), recovering the stomatal response to atmospheric humidity used by a standard empirical approach (Medlyn et al. 2011). However, the stomatal responses to atmospheric \([\text{CO}_2]\) and soil moisture were unrealistic unless \(\lambda\) is a function of both. Manzoni et al. (2013) further advanced the theory by incorporating the soil-plant limitation to leaf water supply and managed to predict realistic stomatal response to soil moisture, but did not consider the response to atmospheric \([\text{CO}_2]\). Thus, a perpetual challenge for the WUEH has been the need to predict \(\lambda\) and its dynamics in response to the full suite of fluctuating environmental stimuli, including \([\text{CO}_2]\).

A recently proposed model assumes that the stomata regulate gas exchange so as...
to maximize the instantaneous carbon gain minus the risk of hydraulic failure by embolism formation (Sperry et al. 2017). The gain and risk of the stomatal opening are given equal weight, each being normalized to start from 0 at stomatal closure (no hydraulic risk but no carbon gain) and rise to 1 as stomata open (maximum photosynthesis but desiccation due to hydraulic failure). This optimization concept predicts realistic theoretic gas exchange response to environmental cues including the response to CO$_2$ and soil moisture stress (Sperry et al. 2017). The gain-risk model has been shown to predict stomatal behavior and plant water status in natural droughts and research garden experiments (Anderegg et al. 2018, Venturas et al. 2018). Importantly, the gain-risk model is based on measurable plant physiological traits and hence directly calculates plant physiological status for any combination of environmental conditions, past or future.

The gain versus risk trade-off algorithm has not been fully tested under elevated [CO$_2$] (Venturas et al. 2018). The atmospheric [CO$_2$], however, is predicted to at least double at 800 ppm by the end of 21 century (RCP8.5, IPCC 2014). Thus, rigorous testing of the algorithm at elevated [CO$_2$] is needed to validate the model predictions of plant responses under novel future environmental conditions.

The goal of the present paper is to evaluate the gain-risk algorithm with particular emphasis on its ability to predict the response to short-term changes in [CO$_2$]. Experiments were conducted in a growth chamber to provide maximal control of environmental conditions. Water birch (*Betula occidentalis* Hook.) was chosen as the study species as it is relatively vulnerable to drought (Sperry and Saliendra 1994). The plants were potted to simplify the modeling of rooting depth and soil water balance. The
growth chamber setting also allowed testing the modeled responses to individual stimuli in isolation ([CO₂], relative humidity, and soil drought), which was not possible to do in the research garden experiment (Venturas et al. 2018). The ability of the gain-risk model to predict the experimental results was compared with a standard empirical stomatal model (Medlyn et al. 2011) parameterized to the best fit the same experimental data.

Materials and Methods

Plant materials

Water birch (Betula occidentalis Hook.) trees were grown from seedlings in the greenhouse of the School of Biological Sciences, University of Utah (40° 45′ 48.75″ N, 111° 50′ 57.66″ W, 1425 m above sea level) starting in October 2016. Each tree was grown in a 5-gallon pot with local sandy clay loam soil. Plants were well watered and day length was regulated to 10 hours from 8:00 am to 6:00 pm with supplemental light (Lucalox LU1000, GE Lighting). In February 2017, two weeks prior to the experiments, ten trees (1—1.5 m tall, 2 years old) were moved into a growth chamber (Model PR-915, Percival Scientific) in order to acclimate the trees to the growth chamber environment. The growth chamber was set at the default settings of ambient CO₂ concentration at 400 ppm, air temperature at 25 °C, relative humidity (RH) at 55%, light intensity (PAR) at 1000 μmol m⁻² s⁻¹, and day length at 10 hours (from 8:00 am to 6:00 pm local time). Trees were watered with 1L water at the end of each day until the drought experiment was initiated.
Experimental design

Growth chamber trees were subjected to three sequential treatments: ambient CO₂ concentration, relative humidity (RH), and soil drought. The responses of leaf xylem pressure and leaf gas exchange were measured during each treatment. The CO₂ treatment was conducted on 6 trees (trees No. 1—6) at a series of ambient CO₂ concentrations starting at 800 ppm, and stepping down to 600, 400, 300, and 200 ppm. All other environmental conditions were kept at default settings. Trees were held at each concentration for at least 90 minutes prior to measurements. The CO₂ response was measured from high to low [CO₂] in order to avoid any legacy impact of cavitation due to more negative leaf xylem pressures at lower [CO₂]. At the end of the experiment, the chamber [CO₂] was returned to the default at 400 ppm.

Next, the RH treatment was conducted on 6 trees (trees No. 1, 2, and 7—10) at a series of relative humidity settings of 75%, 65%, 55%, 45%, and 35% while keeping other environmental conditions at default settings. The actual chamber vapor pressure deficit (air VPD) was estimated for each gas exchange measurement based on spot measurements of RH and air temperature. The humidity response was measured going from high to low RH in order to avoid the potential legacy of cavitation due to lower leaf xylem pressure in drier air. A different set of trees were chosen for the RH (and soil drought, below) treatments to decrease the reduction in leaf area caused by sampling for pressure chamber measurements of xylem pressure. After the RH experiment, the chamber RH was set back to the default 55%.

The final drought response experiment was also performed on six trees (trees No. 2, 4, 6, and 8—10). Trees were watered only on the first day and dried for four successive days.
days, with measurements conducted at the end of the day. After the measurements, trees were bagged and placed in the dark for at least 3 hours to suppress transpiration and equilibrate leaf xylem pressure with soil water potential. Leaf xylem pressure was measured on 2—3 leaves for each bagged tree and served as a proxy for the soil water potential at the end of the day. Trees were then moved back into the growth chamber for further drought. The growth chamber conditions and timing for leaf xylem pressure measurements of the CO₂, RH, and drought treatments are listed in supplementary data Table S1.

The tree response to each treatment (CO₂, RH, soil drought) was assessed from measurements of gas exchange and xylem pressure. Gas exchange measurements were performed only when the light had been turned on for at least 120 minutes and when the growth chamber environment had stabilized for 90 minutes. The whole tree transpiration rate \( (E_{\text{tree}}) \) was measured with a 0.5 g precision 34 kg range balance (Sartorius LP34000P, Sartorius Corporation, Goettingen, Germany). The total weight was recorded to the computer every 10 seconds for 6—10 minutes. Whole tree transpiration rate was estimated from the slope of the linear regression of weight loss vs. time. Leaf level gas exchange (including photosynthetic rate, stomatal conductance, and leaf temperature, \( T_{\text{leaf}} \)) was measured on 2—4 leaves on each tree at each treatment stage with a portable photosynthesis system (Li-6800, LICOR Inc., Lincoln NE, USA) by setting the Li-6800 chamber temperature at the growth chamber temperature. One of the leaves used in the photosynthesis measurement was then used in the leaf xylem pressure measurement with a pressure chamber (PMS Instruments, Corvallis, OR, USA; precision ±0.05 MPa) for each tree at different stages of three treatments. Transpiring leaf xylem pressures were
measured only for three stages in each treatment in order to minimize the disturbance of
decreased leaf area.

Model description

The gain-risk model (Sperry et al. 2017) was modified for the input/output of this
study (Table 1). The model was coded with Julia (Julia 0.4.7, NumFocus) and is publicly
available (https://github.com/Yujie-WANG/Published-Codes-Yujie-WANG). The plant
was represented by one canopy sunlit layer, one stem element, one root layer, and one
rhizosphere and soil layer in series. No shaded canopy layer was modeled because there
was no significant leaf shading for the small saplings (1.0—1.5 m tall) in the growth
chamber, and only one root layer was used due to the homogeneous soil moisture in a
small pot. Leaf temperature was not modeled in this version because the main purpose of
the study was to test the accuracy of the optimization algorithm itself rather than the
additional energy balance routine that predicts $T_{leaf}$ in the full version (Sperry et al. 2017,
Venturas et al. 2018). Instead, the $T_{leaf}$ required by the model was an input and was
averaged from the $T_{leaf}$ measurements for each tree. The model simulations assumed that
cavitation of xylem conduits was irreversible (no xylem refilling). Examples of how
xylem water potential and hydraulic conductivity loss respond to the environmental cues
can be found in Fig. S1.

The gain-risk model calculates the relative photosynthetic gain and hydraulic risk
of stomatal opening at each time step. The gain was the photosynthetic rate relative to the
maximum possible achieved by stomata opening at that time step. Maximal carboxylation
rate at 25 °C ($V_{cmax}$), maximal electron transport at 25 °C ($J_{max}$), air temperature, $T_{leaf}$,
PAR, and ambient \([\text{CO}_2]\) are the necessary inputs for computing the photosynthetic gain (Table 1). The risk function measures the relative loss of hydraulic conductance at the end of the transpiration stream, which rises from 0 at stomatal closure to 1 for complete failure at the runaway cavitation. Necessary inputs include the soil moisture, rhizosphere resistance, vulnerability curves and maximal conductances of the root, stem, and leaf elements of the flow path, as well as the leaf area per basal area (Table 1). Once the gain and risk functions are calculated as a function of stomatal opening, the optimization algorithm finds the point at which the gain minus risk difference is maximized. This predicts the gas exchange and water status parameters (e.g., photosynthetic rate, transpiration rate, leaf xylem pressure) at the time step. Model details can be found in Sperry et al. (2017) and Venturas et al. (2018).

Measuring model input parameters

**Photosynthesis parameters.** \(V_{\text{cmax}}\) and \(J_{\text{max}}\) at 25 °C were obtained from the measured relationship between the photosynthetic rate \((A)\) and inter-cellular \(\text{CO}_2\) concentration \((C_i)\), \(A \sim C_i\) curves. These curves were obtained for each tree in the growth chamber prior to each experimental treatment. For each curve, the net photosynthetic rates were measured at the leaf temperature of 25 °C and light intensity of 1000 \(\mu\text{mol m}^{-2} \text{s}^{-1}\) under a series of \(\text{CO}_2\) concentrations: 50, 100, 150, 200, 300, 400, 500, 600, 800, 1000, 1200, 1400, 1600, 1800 and 2000 ppm. The dark respiration rate was then measured at the leaf temperature of 25 °C and \(\text{PAR}=0\). The gas exchange measurements were done with a portable photosynthesis system (Li-6800). \(A \sim C_i\) curves were fitted to obtain the \(V_{\text{cmax}}\) and \(J_{\text{max}}\) with the `scipy.optimize.leastsq` module in Python 3.6.5 (code provided with
the gain-risk model). Forty-three $A \sim C_i$ curves were constructed for the ten trees and the average $V_{c_{\text{max}}}$ and $J_{\text{max}}$ for each tree were calculated and used as model input. Ambient [CO$_2$] and light were recorded from the growth chamber. Leaf temperatures were recorded from the Li-6800 where the inlet air temperature was set to the chamber air temperature.

**Vulnerability curves for the root and stem.** Vulnerability curves (VCs) of root, stem, and leaf were constructed from well-watered, greenhouse-grown trees of the same cohort for the growth chamber experiments. Branches about 80 cm long and roots were harvested, wrapped with black plastic bags and transported to the lab within 5 minutes of the collection. Stem and root segments about 16 to 20 cm long were cut under water. The segments were vacuum infiltrated in 10 mM KCl for 30 minutes to remove the emboli in vessels. The segments were trimmed to 13.8 cm and maximal hydraulic conductivity was measured with a conductivity apparatus (Sperry et al. 1988). Stem and root segments were then spun in a custom built rotor in a centrifuge for 10 minutes to introduce embolism under different pressures (Alder et al. 1997). Hydraulic conductivity was measured immediately after taking the segment out of the centrifuge by correcting the background flow (Hacke et al. 2000, Torres-Ruiz et al. 2012). Each segment was only used to measure the maximal conductivity and conductivity after spinning in the centrifuge (single spin method, Hacke et al., 2015). Thirty-nine stem segments and twenty-four root segments were used to construct the VCs for stem and root, respectively. Root and stem VCs were fitted to the Weibull function, $k = k_{\text{max}} \times \exp[-(P/B)^{C}]$, where $k_{\text{max}}$ is the maximal hydraulic conductance of the element, $B$ and $C$ are the fitted Weibull parameters and $P$ was the xylem pressure in MPa.
Vulnerability curve for the leaf. Potted trees in the greenhouse were dried to different leaf xylem pressures and then transported to the lab. Leaf xylem pressure was measured on 2—3 bagged leaves for each stressed tree and then a leafy branch (basal diameter > 5mm) was harvested from the tree. Leaf edges were trimmed to expose the minor veins. The hydraulic conductance of the branch \((k_{br})\) was measured using the vacuum chamber method (Kolb et al. 1996). Then leaves were cut from the branches at the proximal base of the petiole and hydraulic conductance of the stem \((k_{st})\) was measured under a series of vacuum pressures. The hydraulic conductance of the leaf xylem was computed as \(k_{lf} = 1 / (1/k_{br} - 1/k_{st})\). The leaf VC was constructed with 31 branches by plotting the \(k_{lf}\) versus leaf xylem pressure and fitting the Weibull function.

Maximal tree hydraulic conductance and its partitioning. The whole tree \(K_{\text{max}}\) per basal area represents the hydraulic conductance in the absence of any embolism. It was back-calculated from measured tree conductance under well-watered conditions, based on the vulnerability curves (Sperry and Love 2015, Venturas et al. 2018). Tree conductance (per growth chamber tree) was the quotient of measured midday transpiration rate and the difference between midday leaf xylem pressure and predawn leaf xylem pressure. The python script to solve for \(K_{\text{max}}\) from measured tree conductance can be found along with the model code.

The \(K_{\text{max}}\) had to be partitioned into root, stem and leaf components (the rhizosphere resistance under wet soil conditions is negligible). The fraction of tree hydraulic resistance (reverse of conductance) in the roots was computed as \((P_{\text{md,b}} - P_{\text{pd}}) / (P_{\text{md}} - P_{\text{pd}})\), where \(P_{\text{pd}}\) is the predawn leaf xylem pressure, \(P_{\text{md,b}}\) is midday bagged leaf xylem pressures of leaves inserted near the root crown, and \(P_{\text{md}}\) is midday xylem...
pressure of transpiring leaves in the canopy. The stem vs. leaf resistance ratio was obtained from the vacuum method, i.e. $k_{lf} / k_{st}$. The resistance ratios of the stem and leaf to the whole tree were calculated as $(P_{md} - P_{md,b}) / (P_{md} - P_{pd}) \times k_{lf} / (k_{lf} + k_{st})$ and $(P_{md} - P_{md,b}) / (P_{md} - P_{pd}) \times k_{st} / (k_{lf} + k_{st})$, respectively.

**Leaf area and stem area.** After the experimental treatments were concluded in the growth chamber, the ten experimental trees were cut to measure the leaf area and stem area. All the shoots were cut from the trees; leaf area and stem area were measured to obtain the leaf area to stem area ratio (La:Ba). Leaf areas were measured with a leaf area meter (Li-3100, LICOR Inc., Lincoln NE, USA). Three out ten trees (tree 3, 5 and 7) had a smaller La:Ba while seven out of ten trees (tree 1, 2, 4, 6, and 8—10) had a bigger La:Ba, so two different average ratios were computed for these two subsets and used as model input. Stem basal area was summed from the shoots in the pot. The average leaf area per basal area and stem basal area per tree were used to convert between leaf area specific vs. whole tree transpiration rate.

**Rhizosphere resistance.** The hydraulic conductance in the rhizosphere ($K_{rhizo}$) cannot be measured directly. The rhizosphere conductance was obtained from the value which minimized the sum of standardized square error (i.e. the sum of $[\text{measured - modeled} / \text{mean measured}]^2$) of leaf xylem pressure, transpiration rate, and photosynthetic rate across all comparisons in the CO$_2$, RH, and drought treatments (90 observations in total).

**Soil moisture.** For the CO$_2$ and RH treatments, “predawn” leaf xylem pressure (a proxy for soil water potential) was measured with a pressure chamber in the early morning before the lights were turned on. Trees were bagged during the night to ensure...
the suppression of nocturnal transpiration. The $P_{pd}$ was measured for each tree in the CO$_2$
and RH treatments and was assumed to be constant throughout the treatment day. For the
drought treatment, the soil water potential was assessed from “predawn” xylem pressures
measured at the end of each drought day as already described.

Testing the gain-risk model

The gain-risk model was run for each tree for the same set of environmental
conditions corresponding to the measurement of the tree's response to CO$_2$, RH, or
drought. The predicted transpiration rate ($E_{tree}$), photosynthetic rate ($A$), and leaf xylem
pressure ($P_{leaf}$) were compared with experimental observations to evaluate the model
performance in predicting the stomatal responses to environmental cues. The comparison
was quantified by calculating the mean absolute error (MAE) and mean absolute
percentage error (MAPE) (mean absolute difference as a percentage of the observed
mean) for each comparison of $A$, $E_{tree}$, and $P_{leaf}$ for each treatment. Errors were equally
weighted across the three variables by studentizing each value (subtracting the observed
mean and dividing by the observed standard deviation). Model performance per treatment
(CO$_2$, RH, soil drought) was averaged from the MAPE for the $A$, $E_{tree}$, and $P_{leaf}$ response
obtained for each treatment. Model performance per variable was the variable's MAPE
averaged over all treatments. The overall model performance was evaluated by the
MAPE averaged across all three variables and treatments.

Comparison with an empirical model

For comparison with the widely used empirical approach for modeling plant water
status and gas exchange, a standard version of Ball-Berry-Leuning-Medlyn type model was used (Ball et al. 1987, Leuning 1995, Medlyn et al. 2011). For the empirical model, stomatal conductance, \( g_s \), was predicted as:

\[
g_s = g_0 + \frac{1.6A}{C_a} \left( 1 + \frac{g_1}{\sqrt{D}} \right) \left( \frac{P_{soil} - P_{min}}{P_{max} - P_{min}} \right), \tag{Eqn 1}
\]

where \( C_a \) is atmospheric [CO\(_2\)], \( D \) is the leaf-to-air vapor pressure deficit, \( g_0, g_1, P_{min}, \) and \( P_{max} \) are four parameters fitted to the data, and \( P_{soil} \) is the soil water potential (predawn leaf xylem pressure was the proxy for \( P_{soil} \)). Standard empirical stomatal conductance models lacks a soil moisture term (e.g. the right-hand bracketed tem; Ball et al. 1987, Leuning 1995, Medlyn et al. 2011), which is added to account for drought stress in large-scale ecosystem models (Trugman et al. 2018b). Equation 1 without the soil moisture term is consistent with the WUEH (Cowan and Farquhar 1977) assuming that RuBP regeneration governs the photosynthesis and marginal water use efficiency is independent of \( C_a \) and \( P_{soil} \). The solution of Eqn 1 must also satisfy the physiological relationship between \( g_s \) and \( A \), which was assumed to be identical to the gain function for consistency with the gain-risk model (\( g_s \) and \( A \) were calculated from the intersection of the \( A \sim C_i \) curve and equation 1). Similarly, \( g_s \) was linked to \( E_{tree} \) and \( P_{leaf} \) as dictated by the risk function. The fitting parameters were optimized to minimize the sum of studentized MAE (measured vs. modeled \( A \), \( E_{tree} \), and \( P_{leaf} \); values were studentized by subtracting the observed mean and dividing by the observed standard deviation) for combined [CO\(_2\)], RH, and drought treatments. Once parameterized, Eqn 1 was numerically solved for the \( g_s \) and associated \( A \), \( E_{tree} \), and \( P_{leaf} \) that satisfied the gain and risk function specific to each tree and measurement period. The code for the empirical model is available at https://github.com/Yujie-WANG/Published-Codes-Yujie-WANG.
Results

Plant traits and model inputs

Mean $V_{cmax}$ for each tree ranged from 12.8 to 96.6 μmol m$^{-2}$ s$^{-1}$ and mean $J_{max}$ ranged from 24.0 to 203.0 μmol m$^{-2}$ s$^{-1}$. $J_{max}$ was linearly correlated with $V_{cmax}$ ($R^2 = 0.992, N = 43$) with a ratio of 1.86 (Fig. S2). Trees No. 3, 5, and 7 had significantly lower leaf area to basal area ratio averaging 2648 m$^2$ m$^{-2}$ compared to the rest of the trees which averaged 5663 m$^2$ m$^{-2}$, and the model was parameterized accordingly. The average percentage of tree hydraulic resistance in root, stem, and leaf pathways was 53.7%, 24.3%, and 22.0%, respectively. Estimated rhizosphere conductance was $6 \times 10^8$ times the $K_{max}$ of each tree (yielding an average rhizosphere resistance of 36.2% over the full range of soil water potential from zero to the value at which gas exchange would cease). The $K_{max}$ of each tree ranged from 560 to 1970 kg h$^{-1}$ MPa$^{-1}$ m$^{-2}$. Roots and leaves were more vulnerable to cavitation than the stems with the $P_{50}$ (xylem pressure at 50% loss of conductance) of -1.14 MPa and -1.10 MPa, respectively, compared to the -1.97 MPa in stems. The traits used for modeling each tree can be found in the supplementary data (Table S2).

Performance of the gain-risk model

In the CO$_2$ experiment, as CO$_2$ concentration was decreased from high (800 ppm) to low (200 ppm), the observed photosynthetic rate decreased ($P < 0.001$, linear regression, Fig. 1A blue data), whole tree transpiration increased non-significantly ($P =$
0.13, linear regression, Fig. 1D blue data), and leaf xylem pressure became more negative 
(P = 0.03, linear regression, Fig. 1G, blue data). The gain-risk model tracked these 
measured trends well (Fig. 1A,D,G, red data). The standardized MAPE was 25.0%, 
averaged across all photosynthesis, transpiration, and leaf xylem pressure comparisons 
(Fig. 2A, Table 2). The error was lower for the predictions of transpiration and xylem 
pressure than for photosynthesis (Table 2). The linear regression slope for modeled vs 
measured transpiration was not significantly different from 1 (P = 0.14, Table 2), and the 
rest of the variable sets had slopes significantly shallower than 1 (P < 0.001, Table 2).

In the RH treatment, as RH was decreased from high to low (from 75% to 35%, 
corresponding to an atmospheric vapor pressure deficit, VPD, ranging from 0.79 kPa to 
2.06 kPa), the observed photosynthetic rate decreased (P < 0.001, linear regression, Fig. 
1B blue data) while tree transpiration rate increased (P = 0.05, linear regression, Fig. 1E 
blue data) and leaf xylem pressure became more negative (P = 0.84, Fig. 1H, blue data). 
The gain-risk model tracked these trends (Fig. 1B,E,H red data) with an overall MAPE of 
21.9% (Fig. 2B). The error was greatest for photosynthesis and least for xylem pressure 
(Table 2). The linear regression slope for each modeled vs measured variable set (i.e. A, 
E_{\text{tree}}, P_{\text{leaf}}, and All) was significantly lower than 1 (P < 0.001, Table 2).

In the soil drought treatment, as predawn xylem pressure fell from -0.5 MPa to 
-2.3 MPa during the drought, the observed photosynthesis, transpiration, and leaf xylem 
pressure fell (P < 0.001, linear regression, Fig. 1C,F,I blue data). These trends were 
predicted by the gain-risk model (Fig. 1C,F,I red data), but the percentage error was 
greater at 41.9% (Fig. 2C). The percentage error was larger for photosynthesis and 
transpiration than xylem pressure (Table 2). The larger percentage error in the drought
treatment compared to the CO₂ and RH treatments resulted from the lower mean 
photosynthesis and transpiration rates measured under drought stress. In terms of average 
absolute value of the error, the drought treatment was comparable to the [CO₂] and RH 
treatments. The linear regression slopes for the modeled vs measured transpiration and 
leaf xylem pressure were not significantly different from 1 (P = 0.58 and 0.13, 
respectively, Table 2), but the slopes for photosynthesis and combined variable set were 
significantly lower than 1 (P < 0.001, Table 2).

Pooling the CO₂, RH, and soil drought treatments, the overall MAPE for the gain 
risk model was 26.8% (Fig. 2D), with more error in the photosynthesis prediction (38.1%) 
than the xylem pressure prediction (14.5%). Transpiration was intermediate (27.8%, 
Table 2). The model predictions fell close to the 1:1 line which was also within the 95% 
confidence limits of the regression. A linear regression of the studentized model 
prediction versus observations had slope lower than 1 for each treatment, each variable, 
and combined treatments (P < 0.01, Fig. 2A—D, Table 2).

**Comparison with the empirical model**

Pooling across all treatments and variables, the gain-risk model predicted 
observed tree responses more skillfully (MAPE = 26.8%) than the Ball-Berry-Leuning-
Medlyn empirical model (MAPE = 37.5%; Fig. 2D,H). On a per treatment basis, the 
gain-risk model gave lower errors for all the [CO₂], RH, and drought responses (Fig. 
2A—C,E—G). Per variable, the gain-risk model better predicted the photosynthesis, 
whole tree transpiration, and leaf xylem pressure for combined treatments. The empirical 
model only performed slightly better for photosynthesis in the [CO₂] treatment and whole
tree transpiration in the drought treatment (Table 2). A linear regression of the studentized empirical fitting had slope lower than 1 for each treatment and combined treatments (P < 0.001, Fig. 2E—H, Table 2). Per variable, only the linear regression for leaf xylem pressure in the RH, drought and all treatments combined showed slopes not significantly different from 1 (P = 0.34, 0.91, and 0.76, respectively, Table 2). In the RH treatment, the empirical model underestimated $A, E_{\text{tree}},$ and $P_{\text{leaf}}$ as the modeled values were below the 1:1 line (Fig. 2F).

Discussion

The gain-risk optimization model was able to capture the $[\text{CO}_2]$, air humidity, and soil drought responses in novel conditions, suggesting that patterns of tree-level gas exchange are consistent with an optimization of carbon gain and hydraulic risk. The gain-risk model showed better overall predicting power than the empirical model, which had the advantage of freely tuning four parameters to best fit the data. The only parameter adjusted post-hoc in the gain-risk approach was the rhizosphere conductance, which is a difficult trait to measure. This trait selectively influences the model under drought conditions because only in drying soil does rhizosphere hydraulic conductance become limiting (Sperry et al. 1998, Sperry and Love 2015, Wolfe et al. 2016). Thus, the post-hoc adjustment of the rhizosphere conductance had a minimal influence on the good fits observed in the well-watered $\text{CO}_2$ and RH treatments. The advantage of having all model parameters associated with identifiable traits is that this makes it easier to assign a value and uncertainty to them \textit{a priori} when true predictions are required (as opposed to the
hind-casting that is possible during model validation). One can also better understand the physiological basis for uncertainties in model projections when all inputs are linked to trait and process. At the same time, it is important to restrict the model to well understood trait and process, or risk regression to post-hoc fitting that becomes equivalent to the empirical approach. For example, it can be conceptually useful to incorporate phloem transport in an optimization model, but this approach has the downside of adding a suite of currently poorly known parameters (Nikinmaa et al. 2013, Huang et al. 2018).

The present results add to the prior validations of the gain-risk algorithm in controlled plantation experiment with aspen (\textit{Populus tremuloides}, Venturas et al. 2018), and meta-analysis of gas exchange data from a variety of species (Anderegg et al. 2018). The work adds to this body of literature and is the first testing of the model’s CO2 response to both elevated and decreased CO2 concentrations. The overall error (26.8% for all treatments) was comparable to that for the Venturas et al. (2018) study (27.9% for control and drought treatments). Although the percentage error was higher for the drought treatment (41.9%), this was owing to lower mean values rather than to a greater absolute error. The MAEs for water birch (A: 2.83, $E_{\text{tree}}$: 135.52, and $P_{\text{leaf}}$: 0.23 for drought treatment, units in Table 1) were comparable to the MAEs for aspen in the Venturas study (A: 2.3, $E_{\text{tree}}$: 151.2, and $P_{\text{leaf}}$: 0.4, units in Table 1). An advantage of the growth chamber experiments was the ability to isolate the model error for each individual driver ([CO2], relative humidity, and soil drought). Similar absolute error values indicated that the gain-risk model represented all responses with equal fidelity (Table 2).

The slope of the model predictions and observations in Fig. 2D was significantly lower than one, suggesting that the model either underestimated gas exchange rates under
favorable conditions or overestimated them under stressful conditions. The results suggest the latter case applies to the water birch because the model predicted leaf xylem pressure became overly negative under stressed conditions (Fig. 1F,1I,2C). This behavior would occur if the measured leaf VC was more resistant than the actual leaf VC. An overly resistant leaf VC would lead to more negative predicted $P_{\text{leaf}}$ and higher predicted transpiration at any soil moisture condition (Fig. 1F,1I,2C). The measured leaf VC was for leaf xylem only, and so excluded potential declines in leaf hydraulic conductance in the extra-xylary flow path. The response of extra-xylary hydraulic conductance to water stress requires more quantitative investigation (Bartlett et al. 2014, Meinzer et al. 2016, Scoffoni et al. 2017) and may improve model performance. Incorporating the mesophyll conductance in the model may also improve the predictions (Flexas et al. 2008, Dewar et al. 2018), but there are still knowledge gaps that prevent incorporating it in the gain-risk model such as how to quantify the change of $G_M$ in response to the environment.

The empirical approach performed less satisfactorily compared to the trait-based gain-risk model, especially in predicting $E_{\text{tree}}$ and $P_{\text{leaf}}$ in the CO$_2$ and RH treatments (Table 2). The underperformance of the empirical model was despite the advantage of fitting model parameters to the observed data set and using the same linkage between $g_s$, $A$, $E_{\text{tree}}$, and $P_{\text{leaf}}$ employed in the gain-risk model (i.e. the gain and risk functions). Either the model “parameters” are not constants as intended, or the empirical equation itself does not fully capture the complexity of the stomatal response to CO$_2$, RH, and soil drought. Even if an empirical approach had been as successful as the gain-risk model, as was the case in the aspen study of Venturas et al. (2018), the gain-risk model has the advantage of being parameterized by measurable traits with known uncertainties. The

While the gain-risk model can predict well the stomatal behavior based on measured traits, the predictions may only be relevant for short timeframes when these measured traits stay unchanged. Acclimation such as changes in leaf respiration, leaf area per basal area, photosynthetic capability, and rooting depth has the potential to change plant response over time to the long-term changes in [CO₂], temperature, and other factors (Eissenstat et al. 2000, Ainsworth and Long 2005, Guswa 2008). The fact that the gain-risk model is trait-based allows for modeling these acclimation processes as they become better understood. In conclusion, the gain-risk model appears to hold promise for improving predictions of forest health in response to a changing climate.

Acknowledgments

This study was funded by NSF 1450650 granted to John S. Sperry. W.R.L.A. acknowledges funding from the David and Lucille Packard Foundation, the University of Utah Global Change and Sustainability Center, NSF Grants 1714972 and 1802880, and the USDA National Institute of Food and Agriculture, Agricultural and Food Research Initiative Competitive Programme, Ecosystem Services and Agro-ecosystem Management, Grant No. 2018-67019-27850. A.T.T. acknowledges support from the USDA National Institute of Food and Agriculture Postdoctoral Research Fellowship Grant No. 2017-07164.
References


Anderegg WRL, Klein T, Bartlett M, Sack L, Pellegrini AFA, Choat B (2016) Meta-analysis reveals that hydraulic traits explain cross-species patterns of drought-


Hacke UG, Sperry JS, Pittermann J (2000) Drought experience and cavitation resistance
in six shrubs from the Great Basin, Utah. Basic Appl. Ecol. 1:31–41


De Kauwe MG, Medlyn BE, Zaehle S, Walker AP, Dietze MC, Hickler T, Jain AK, Luo


Meinzer FC, Woodruff DR, Marias DE, Smith DD, McCulloh KA, Howard AR,


Sperry JS, Donnelly JR, Tyree MT (1988) A method for measuring hydraulic...
conductivity and embolism in xylem. Plant, Cell Environ. 11:35–40


**Figures Legends**

**Fig. 1** Observations and gain-risk model predictions in the CO₂, humidity, and drought treatments. The blue numbers show the observations while the red numbers show the model prediction of each tree (identification number from 1—10). Panels A, B, and C show the observed and modeled photosynthetic rate (A). Panels D, E, and F show the observed and modeled tree transpiration (E<sub>tree</sub>). Panels G, H, and I show the observed and modeled leaf xylem pressure (P<sub>leaf</sub>). The VPD is the vapor pressure deficit in the air.
Fig. 2 Comparison of model predictions of studentized photosynthesis ($A$, green circle), transpiration ($E_{\text{tree}}$, blue square), and leaf xylem pressure ($P_{\text{leaf}}$, red triangle) versus experimental observations. Panels A, B, C, and D show the gain-risk model predictions for CO$_2$, RH, drought, and all treatments, respectively. Panels E, F, G, and H show the empirical model fittings for CO$_2$, RH, drought, and all treatments, respectively. Solid black lines are the 1:1 relationship. Dashed lines are the regression lines. Dotted lines are the 95% confidence intervals for the linear regression. The mean absolute percentage error and the regression statistics are listed in Table 2.
Table 1 List of symbols, definitions, and status as model input or output. Note that leaf temperature and soil water potential are used as input in this model to test the gain-risk algorithm while they are used as outputs in other versions of the model (Venturas et al. 2018).

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Unit</th>
<th>Input / Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>( A )</td>
<td>Photosynthetic assimilation, photosynthetic rate</td>
<td>( \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1} )</td>
<td>Output</td>
</tr>
<tr>
<td>( C_a )</td>
<td>Atmospheric CO(_2) concentration</td>
<td>ppm</td>
<td>Input</td>
</tr>
<tr>
<td>( C_i )</td>
<td>Inter-cellular CO(_2) concentration</td>
<td>ppm</td>
<td>Output</td>
</tr>
<tr>
<td>( D )</td>
<td>Leaf-to-air vapor pressure deficit</td>
<td>kPa</td>
<td>-</td>
</tr>
<tr>
<td>( E_{\text{tree}} )</td>
<td>Transpiration rate of the tree per basal area</td>
<td>kg h(^{-1}) m(^{-2})</td>
<td>Output</td>
</tr>
<tr>
<td>( J_{\text{max}} )</td>
<td>Maximal electron transport at 25 °C</td>
<td>( \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1} )</td>
<td>Input</td>
</tr>
<tr>
<td>( K_{\text{max}} )</td>
<td>Maximal tree hydraulic conductance</td>
<td>kg h(^{-1}) MPa(^{-1}) m(^{-2})</td>
<td>Input</td>
</tr>
<tr>
<td>( K_{\text{rhizo}} )</td>
<td>Maximal tree rhizosphere conductance</td>
<td>kg h(^{-1}) MPa(^{-1}) m(^{-2})</td>
<td>Input</td>
</tr>
<tr>
<td>La:Ba</td>
<td>Leaf area to basal area ratio</td>
<td>m(^2) m(^{-2})</td>
<td>Input</td>
</tr>
<tr>
<td>MAPE</td>
<td>Mean absolute percent error</td>
<td>%</td>
<td>-</td>
</tr>
<tr>
<td>PAR</td>
<td>Photosynthetic active radiation</td>
<td>( \mu\text{mol m}^{-2} \text{ s}^{-1} )</td>
<td>Input</td>
</tr>
<tr>
<td>( P_{\text{leaf}} )</td>
<td>Leaf xylem pressure under light condition</td>
<td>MPa</td>
<td>Output</td>
</tr>
<tr>
<td>( P_{pd} )</td>
<td>Predawn leaf xylem pressure, a proxy for</td>
<td>MPa</td>
<td>-</td>
</tr>
</tbody>
</table>
soil water potential

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Unit</th>
<th>Input</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{soil}$</td>
<td>Soil water potential</td>
<td>MPa</td>
<td>Input</td>
</tr>
<tr>
<td>RH</td>
<td>Relative humidity</td>
<td>%</td>
<td>-</td>
</tr>
<tr>
<td>$T_{leaf}$</td>
<td>Leaf temperature</td>
<td>ºC</td>
<td>Input</td>
</tr>
<tr>
<td>VC</td>
<td>Xylem vulnerability curve to cavitation</td>
<td>-</td>
<td>Input</td>
</tr>
<tr>
<td>$V_{cmax}$</td>
<td>Maximal carboxylation rate at 25 ºC</td>
<td>µmol CO$_2$ m$^{-2}$ s$^{-1}$</td>
<td>Input</td>
</tr>
<tr>
<td>VPD</td>
<td>Vapor pressure deficit in the air</td>
<td>kPa</td>
<td>Input</td>
</tr>
<tr>
<td>Weibull $B$</td>
<td>Fitting parameter of the VC Weibull function</td>
<td>-MPa</td>
<td>Input</td>
</tr>
<tr>
<td>Weibull $C$</td>
<td>Fitting parameter of the VC Weibull function</td>
<td>-</td>
<td>Input</td>
</tr>
</tbody>
</table>
Table 2 The comparison of gain-risk model and empirical model predictions. MAE (units for A, $E_{\text{tree}}$, and $P_{\text{leaf}}$ reported in Table 1) and MAPE stand for mean absolute error and mean absolute percentage error, respectively. The row “Slope” denotes the slope of the regression between observed values (x) and modeled values (y). The row “Slope = 1” denotes the P-value for the linear regression slope being different from 1. Units as in Table 1.

<table>
<thead>
<tr>
<th>Treatment</th>
<th>Parameter</th>
<th>$A$</th>
<th>$E_{\text{tree}}$</th>
<th>$P_{\text{leaf}}$</th>
<th>All</th>
</tr>
</thead>
<tbody>
<tr>
<td>/</td>
<td>MAPE</td>
<td>41.1%</td>
<td>17.8%</td>
<td>16.2%</td>
<td>25.0%</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>MAE</td>
<td>4.25</td>
<td>78.83</td>
<td>0.18</td>
<td></td>
</tr>
<tr>
<td>/</td>
<td>Slope</td>
<td>0.62±0.11</td>
<td>0.81±0.12</td>
<td>0.25±0.15</td>
<td>0.61±0.08</td>
</tr>
<tr>
<td>Gain-Risk</td>
<td>Slope = 1</td>
<td>0.00</td>
<td>0.14</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td></td>
<td>$R^2$</td>
<td>0.527</td>
<td>0.606</td>
<td>0.140</td>
<td>0.441</td>
</tr>
<tr>
<td>/</td>
<td>MAPE</td>
<td>40.7%</td>
<td>49.1%</td>
<td>26.7%</td>
<td>38.8%</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>MAE</td>
<td>4.21</td>
<td>217.29</td>
<td>0.30</td>
<td></td>
</tr>
<tr>
<td>/</td>
<td>Slope</td>
<td>0.63±0.11</td>
<td>0.36±0.16</td>
<td>-0.23±0.24</td>
<td>0.33±0.12</td>
</tr>
<tr>
<td>Empirical</td>
<td>Slope = 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td></td>
<td>$R^2$</td>
<td>0.539</td>
<td>0.155</td>
<td>0.059</td>
<td>0.094</td>
</tr>
<tr>
<td>RH</td>
<td>MAPE</td>
<td>31.5%</td>
<td>23.5%</td>
<td>10.7%</td>
<td>21.9%</td>
</tr>
<tr>
<td>/</td>
<td>MAE</td>
<td>3.50</td>
<td>111.66</td>
<td>0.12</td>
<td></td>
</tr>
<tr>
<td>Gain-Risk</td>
<td>Slope</td>
<td>0.45±0.08</td>
<td>0.25±0.07</td>
<td>0.71±0.11</td>
<td>0.43±0.07</td>
</tr>
<tr>
<td></td>
<td>Slope = 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>----------------------</td>
<td>-----------</td>
<td>-----</td>
<td>-----</td>
<td>-----</td>
<td></td>
</tr>
<tr>
<td></td>
<td>0.00</td>
<td>0.00</td>
<td>0.02</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.563</td>
<td>0.287</td>
<td>0.708</td>
<td>0.332</td>
<td></td>
</tr>
<tr>
<td>MAPE</td>
<td>46.9%</td>
<td>41.7%</td>
<td>14.0%</td>
<td>34.2%</td>
<td></td>
</tr>
<tr>
<td>RH</td>
<td>5.20</td>
<td>198.18</td>
<td>0.16</td>
<td></td>
<td></td>
</tr>
<tr>
<td>/ Slope</td>
<td>0.45±0.07</td>
<td>0.37±0.12</td>
<td>0.85±0.16</td>
<td>0.51±0.07</td>
<td></td>
</tr>
<tr>
<td>Empirical Slope = 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.34</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.632</td>
<td>0.237</td>
<td>0.651</td>
<td>0.382</td>
<td></td>
</tr>
<tr>
<td>MAPE</td>
<td>43.0%</td>
<td>65.4%</td>
<td>17.3%</td>
<td>41.9%</td>
<td></td>
</tr>
<tr>
<td>Drought MAE</td>
<td>2.83</td>
<td>135.52</td>
<td>0.23</td>
<td></td>
<td></td>
</tr>
<tr>
<td>/ Slope</td>
<td>0.44±0.10</td>
<td>0.91±0.17</td>
<td>0.85±0.10</td>
<td>0.71±0.09</td>
<td></td>
</tr>
<tr>
<td>Gain-Risk Slope = 1</td>
<td>0.00</td>
<td>0.58</td>
<td>0.13</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.421</td>
<td>0.544</td>
<td>0.849</td>
<td>0.483</td>
<td></td>
</tr>
<tr>
<td>MAPE</td>
<td>45.5%</td>
<td>59.2%</td>
<td>21.7%</td>
<td>42.1%</td>
<td></td>
</tr>
<tr>
<td>Drought MAE</td>
<td>2.99</td>
<td>122.56</td>
<td>0.29</td>
<td></td>
<td></td>
</tr>
<tr>
<td>/ Slope</td>
<td>0.36±0.08</td>
<td>0.45±0.12</td>
<td>1.02±0.20</td>
<td>0.55±0.09</td>
<td></td>
</tr>
<tr>
<td>Empirical Slope = 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.91</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.446</td>
<td>0.373</td>
<td>0.658</td>
<td>0.381</td>
<td></td>
</tr>
<tr>
<td>MAPE</td>
<td>38.1%</td>
<td>27.8%</td>
<td>14.5%</td>
<td>26.8%</td>
<td></td>
</tr>
<tr>
<td>All MAE</td>
<td>3.58</td>
<td>106.58</td>
<td>0.17</td>
<td></td>
<td></td>
</tr>
<tr>
<td>/ Slope</td>
<td>0.56±0.07</td>
<td>0.54±0.05</td>
<td>0.79±0.07</td>
<td>0.60±0.04</td>
<td></td>
</tr>
<tr>
<td>Gain-Risk Slope = 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.01</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.463</td>
<td>0.541</td>
<td>0.690</td>
<td>0.506</td>
<td></td>
</tr>
<tr>
<td>All MAPE</td>
<td>44.2%</td>
<td>47.6%</td>
<td>20.7%</td>
<td>37.5%</td>
<td></td>
</tr>
<tr>
<td>Method</td>
<td>MAE</td>
<td>Slope</td>
<td>Slope = 1</td>
<td>$R^2$</td>
<td></td>
</tr>
<tr>
<td>--------------</td>
<td>------</td>
<td>---------------------</td>
<td>-----------</td>
<td>--------</td>
<td></td>
</tr>
<tr>
<td>Empirical</td>
<td>4.17</td>
<td>0.51±0.06</td>
<td>0.25±0.07</td>
<td>0.95±0.15</td>
<td>0.51±0.05</td>
</tr>
<tr>
<td>Slope = 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.76</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.479</td>
<td>0.153</td>
<td>0.455</td>
<td>0.304</td>
<td></td>
</tr>
</tbody>
</table>